

An overview of the metafor package with some interesting applications

Society for Research Synthesis Methodology
Annual Conference 2021
Olkin Award Presentation

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2021-07-01

First of all ...

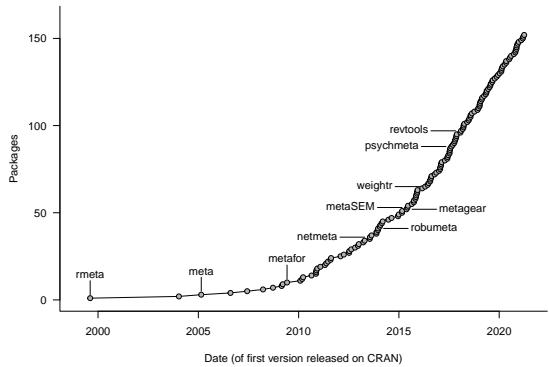
- thank you!
- would like to talk about the development of metafor
- highlight some interesting applications
- next SRSM talk will start in around 365 — 2 days
- hence: my timelimit for this talk is around 8712 hours!



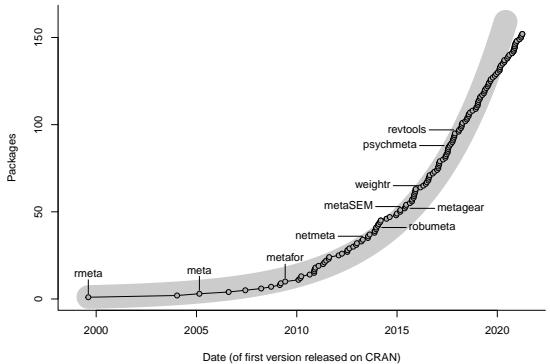
Software for Meta-Analysis: Early Developments

- 1990's: DSTAT [1], True Epistat [2], FAST*PRO [3], macros, ...
- 1993: RevMan released (not R) [4]
- 1997: MetaWin released (also not R) [5]
- 1998: Comprehensive Meta-Analysis released (still no R) [6]
- 1999: rmeta package, but no 'meta-regression' capabilities
- ~2000: wrote function for fitting random/mixed-effects models
- ~2005: put function on my personal website
- ~2005: meta package
- 2006-2009: a few other packages
- 2009: published metafor package
- 2009-now: lots of new packages (current count: 152)
based on CRAN Task View on Meta-Analysis:
<https://cran.r-project.org/view=MetaAnalysis>

First Releases of Meta-Analysis R Packages



Exponential Growth (might be slowing down)



Development of the metafor Package

- first version (0.5-0) released 2009-06-04
- a total of 30 versions released so far
- latest is 3.0-1 released 2021-06-02
- added various illustrative datasets over the years (60 as of now)
- added various outcome measures over the years (60 as of now)
- full changelog:
<https://wviechtb.github.io/metafor/news/index.html>

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Some Milestones

Version	Date	Notes / Changes
0.5-0	2009-06-04	• first version released on CRAN • <code>rma.uni()</code> , <code>rma.mh()</code> , <code>rma.peto()</code>
0.5-4	2009-09-18	• <code>regtest()</code> and <code>ranktest()</code> functions • <code>anova()</code> function (LRTs, contrasts)
0.5-5	2009-10-08	• <code>cumul()</code> and <code>leave1out()</code> functions
0.5-7	2009-12-06	• <code>permuteest()</code> function
1.0-1	2010-02-02	• version 1 released
1.4-0	2010-07-30	• various improvements for JSS paper 2010-08-05 • JSS paper published [7]
1.5-0	2010-12-16	• started metafor website
1.7-0	2013-02-06	• <code>rma.glmm()</code> function

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Some Milestones

Version	Date	Notes / Changes
1.9-2	2013-10-07	• <code>rma.mv()</code> and <code>profile()</code> functions
1.9-3	2014-05-05	• models with user-defined weights • sparse matrices for <code>rma.mv()</code> • autoregressive structures for <code>rma.mv()</code>
1.9-6	2015-05-07	• multiple correlated random effects • parallel processing for <code>profile()</code>
1.9-8	2015-09-28	• <code>robust()</code> function
1.9-9	2016-09-25	• started using git and GitHub • <code>ranef()</code> and <code>gosh()</code> functions • permutation-based CIs of model coefficients

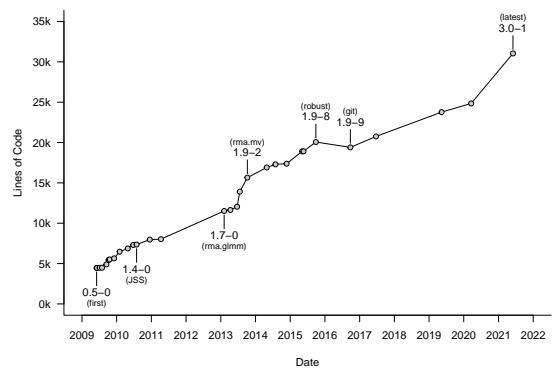
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Some Milestones

Version	Date	Notes / Changes
2.1-0	2019-05-13	• <code>reporter()</code> function • cluster-level outlier/influence statistics • more parallel processing capabilities • spatial correlation structures
2.4-0	2020-03-19	• <code>to.wide()</code> and <code>contrmat()</code> for NMA
3.0-2	2021-06-09	• <code>selmodel()</code> , <code>tes()</code> , PET/PESE • location-scale models

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Lines of Code



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Package Features: Effect Sizes and Outcome Measures

- measures for 2x2 table data (e.g., RD, RR, OR)
- measures for two-group person-time data (e.g., IRR, IRD)
- raw/standardized mean differences and response ratios
- conversions of 2x2 table data / ORs to SMDs and vice-versa
- raw and Fisher's r-to-z transformed correlation coefficients
- (semi)partial correlations and biserial/tetrachoric correlations
- proportions and transformations thereof
- incidence rates and transformations thereof
- raw/standardized mean change measures
- measures of change in 2x2 table data
- reliability measures (Cronbach's alpha and transformations)
- measures to quantify variability (and group differences thereof)

Package Features: Models and Analysis Approaches

- fixed-, random-, and mixed-effects (meta-regression) models
- Mantel-Haenszel and Peto's (one-step) method
- generalized linear (mixed-effects) models
- multilevel and multivariate meta-analytic models
- network meta-analysis / mixed treatment comparisons
- phylogenetic meta-analysis
- spatio-temporal meta-analytic models
- models with user-defined weights
- location-scale models

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Package Features: Plots and Figures

- forest plots
 - funnel plots
 - bubble plots
 - Baujat plots
 - L'Abbé plots
 - radial (Galbraith) plots
 - GOSH plots
 - profile likelihood plots
 - normal quantile-quantile plots

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Package Features: Publication Bias

- rank correlation test
 - Egger's regression test (PET / PEESE methods)
 - trim and fill method
 - Henmi and Copas approach
 - file drawer analysis
 - test of excess significance
 - selection models (some of which don't suck)

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Package Features: Inference Methods

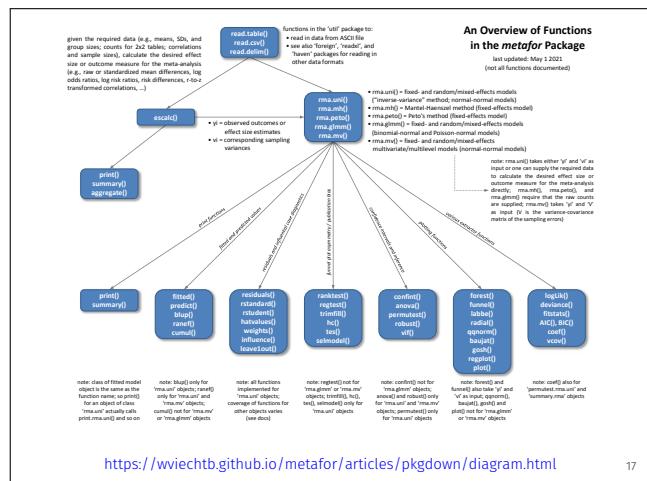
- Wald-type and likelihood ratio tests
 - Knapp and Hartung method
 - prediction intervals
 - confidence intervals for heterogeneity statistics
 - permutation tests / confidence intervals
 - (cluster) robust tests and confidence intervals
 - cumulative meta-analysis
 - best linear unbiased predictions
 - model fit / information criteria criteria
 - bootstrapping (via `boot` package) ([website](#))
 - multimodel inference (via `glmulti` package) ([website](#))
 - multiple imputation (via `mice` package) ([website](#))

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Package Features: Outlier and Influence Diagnostics

- raw, standardized, and studentized residuals
 - DFFITS, DFBETAS values, Cook's distances, covariance ratios
 - cluster-level outlier/influence statistics
 - model weights and hat values
 - leave-one-out analyses

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Demo: Random-Effects Model

```
# load metafor package  
library(metafor)
```

```
# look at the BCG dataset  
dat_bcg
```

trial	author	year	tpos	tneg	cpos	cneg	ablat	alloc
1	Aronson	1948	4	119	11	128	44	random
2	Ferguson & Simes	1949	6	300	29	274	55	random
3	Rosenthal et al	1960	3	228	11	209	42	random
4	Hart & Sutherland	1977	62	1536	248	12619	52	random
5	Frimodt-Møller et al	1973	33	5036	47	5761	13	alternate
6	Stein & Aronson	1953	180	1361	372	1079	44	alternate
7	Vandiviere et al	1973	8	2537	10	619	19	random
8	TPT Madras	1980	505	87886	499	87892	13	random
9	Coetze & Berjak	1968	29	7470	45	7232	27	random
10	Rosenthal et al	1961	17	1699	65	1600	42	systematic
11	Comstock et al	1974	186	50448	141	27197	18	systematic
12	Comstock & Webster	1969	5	2493	3	2338	33	systematic
13	Comstock et al	1976	27	16886	29	17825	33	systematic

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Demo: Random-Effects Model

```
# calculate log risk ratios and corresponding sampling variances
dat <- escalc(measure="RR", ai=tpos, bi=tneg,
              ci=tpos, di=cneg, data=dat.bcg)
dat
```

trial	author	year	...	yi	vi
1	Aronson	1948	...	-0.8893	0.3256
2	Ferguson & Simes	1949	...	-1.5854	0.1946
3	Rosenthal et al	1960	...	-1.3481	0.4154
4	Hart & Sutherland	1977	...	-1.4416	0.0200
5	Frimodt-Møller et al	1973	...	-0.2175	0.0512
6	Stein & Aronson	1953	...	-0.7861	0.0069
7	Vandiviere et al	1973	...	-1.6209	0.2230
8	TPT Madras	1980	...	0.0120	0.0040
9	Coetze & Berjak	1968	...	-0.4694	0.0564
10	Rosenthal et al	1961	...	-1.3713	0.0730
11	Comstock et al	1974	...	-0.3394	0.0124
12	Comstock & Webster	1969	...	0.4459	0.5325
13	Comstock et al	1976	...	-0.0173	0.0714

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Demo: Random-Effects Model

```
# random-effects model (using log risk ratios and variances as input)
res <- rma(yi, vi, data=dat)
res

## Random-Effects Model (k = 13; tau^2 estimator: REML)
##
## tau^2 (estimated amount of total heterogeneity): 0.3132 (SE = 0.1664)
## tau (square root of estimated tau^2 value):      0.5597
## I^2 (total heterogeneity / total variability):   92.22%
## H^2 (total variability / sampling variability): 12.86
##
## Test for Heterogeneity:
## Q(df = 12) = 152.2330, p-val < .0001
##
## Model Results:
##
## estimate      se     zval    pval   ci.lb   ci.ub
## -0.7145  0.1798 -3.9744 <.0001 -1.0669 -0.3622
```

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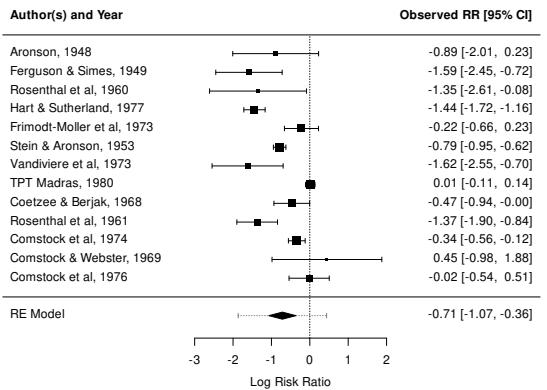
Demo: Random-Effects Model

```
# then do lots more stuff ...
forest(res)
funnel(res)
influence(res)
plot(influence(res))
leave1out(res)
baujat(res)
ranktest(res)
regtest(res)
trimfill(res)
funnel(trimfill(res))
cumul(res)
forest(cumul(res))
radial(res)
labbe(res)
plot(gosh(res))
selmodel(res)

# note: the following plots are based on various datasets
```

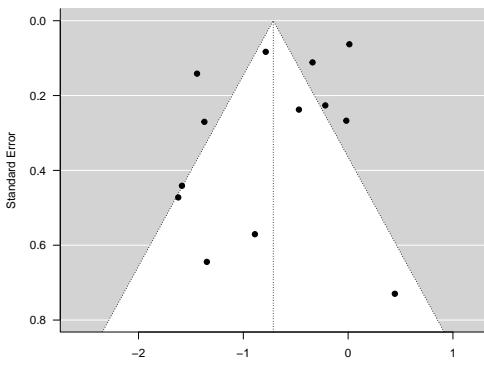
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Demo: Forest Plot

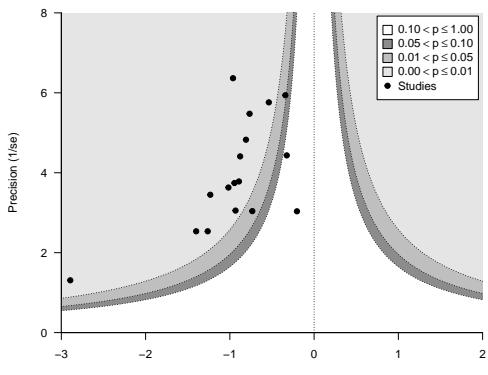


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Demo: Funnel Plot



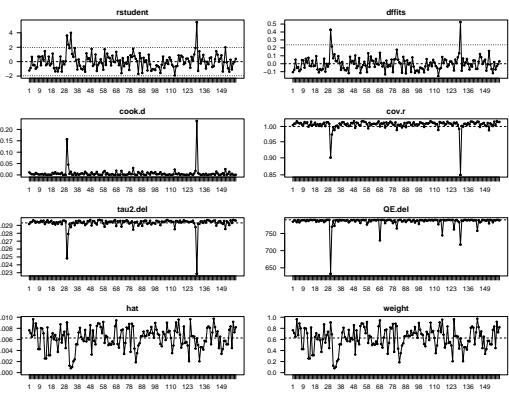
Demo: Contour-Enhanced Funnel Plot [8]



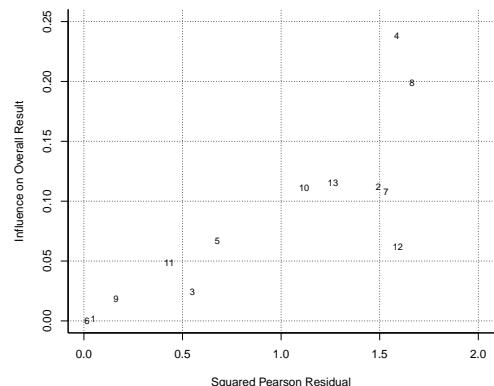
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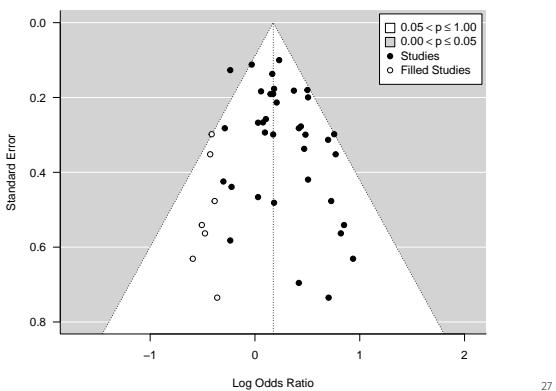
Demo: Outlier / Influence Diagnostics [9, 10]



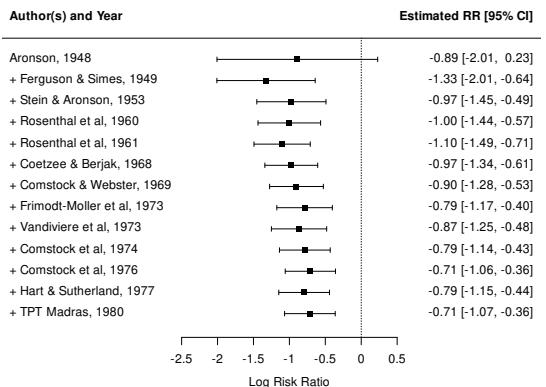
Demo: Baujat Plot [10, 11]



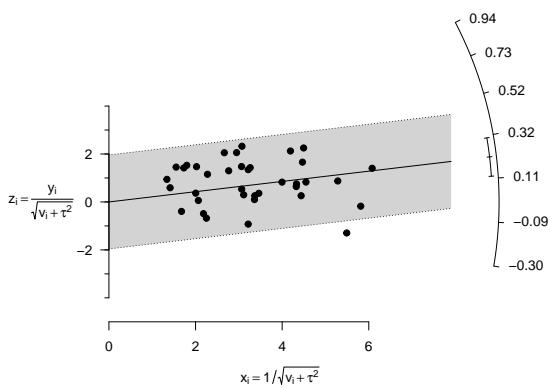
Demo: Trim-and-Fill [12, 13]



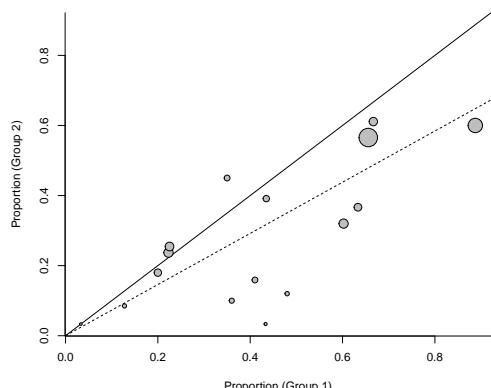
Demo: Cumulative Meta-Analysis [14]



Demo: Radial (Galbraith) Plot [15]



Demo: L'Abbé Plot [16]



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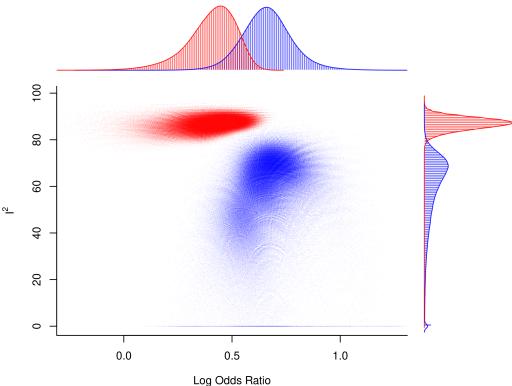
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Demo: GOSH Plot [17]



Demo: Meta-Regression

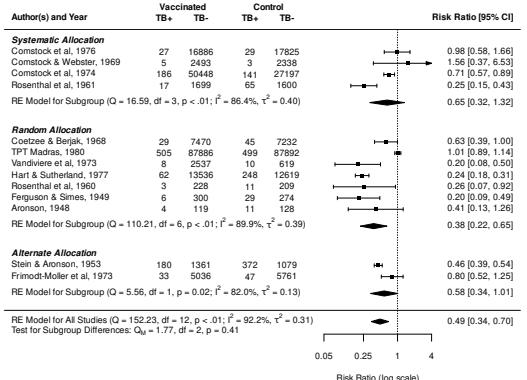
```
# mixed-effects meta-regression model
res <- rma(yi, vi, mods = ~ ablat + alloc, data=dat)
res

## Mixed-Effects Model (k = 13; tau^2 estimator: REML)
##
## tau^2 (estimated amount of residual heterogeneity): 0.1446
## tau (square root of estimated tau^2 value): 0.3803
## I^2 (residual heterogeneity / unaccounted variability): 70.11%
## H^2 (unaccounted variability / sampling variability): 3.35
## R^2 (amount of heterogeneity accounted for): 53.84%
##
## Test for Residual Heterogeneity:
## QE(df = 9) = 26.2034, p-val = 0.0019
## ...
## ...
```

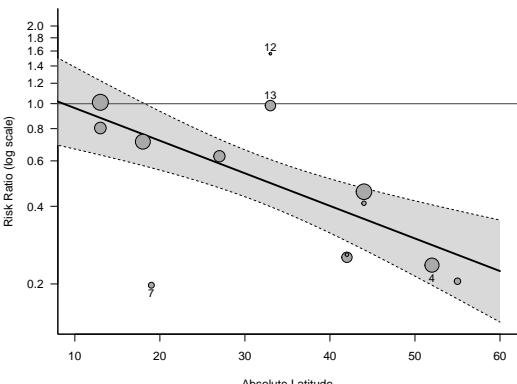
Demo: Meta-Regression

```
## ...
##
## Test of Moderators (coefficients 2:4):
## QM(df = 3) = 11.0605, p-val = 0.0114
##
## Model Results:
##
##          estimate      se     zval    pval   ci.lb   ci.ub
## intrcpt  0.2932  0.4050  0.7239  0.4691 -0.5006  1.0870
## ablat    -0.0273  0.0092 -2.9650  0.0030 -0.0453 -0.0092
## allocrand -0.2675  0.3504 -0.7633  0.4453 -0.9543  0.4193
## allocsystemic 0.0585  0.3795  0.1540  0.8776 -0.6854  0.8023
```

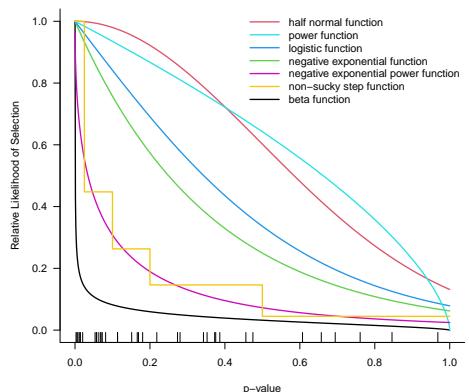
Demo: Forest Plot with Subgroups



Demo: Meta-Analytic Scatterplot [18]



Demo: Selection Models [19–21]



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The reporter() Function

- automatically generates a report based on `rma.uni` objects
- describes the statistical methods used
- gives a natural language summary of the results
- includes a forest and a funnel plot
- gives references for all methods used
- output can be html, pdf, or docx

Demo: Using reporter()

```
dat <- escalc(measure="RR", ai=tpos, bi=tneg,
               ci=cpos, di=cneg,
               slab=paste(author, " ", " ", year, sep=""),
               data=dat.bcg)
res <- rma(yi, vi, data=dat)
reporter(res)
```

Directory for generating the report is: /tmp/Rtmpusq5ns

Copying references.bib and apa.csl to report directory ...
 Saving model object to report_res.rdata ...
 Creating report_res.rmd file ...
 Rendering report_res.rmd file ...
 Generated /tmp/Rtmpusq5ns/report_res.html ...
 Opening report ...

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Demo: Using reporter()

Analysis Report

Generated with the reporter() Function of the metafor Package

19 January, 2021

Methods

The analysis was carried out using the log risk ratio as the outcome measure. A random-effects model was fitted to the data. The amount of heterogeneity (i.e., τ^2) was estimated using the restricted maximum-likelihood estimator (Viechtbauer, 2005). In addition to the estimate of τ^2 , the Q -test for heterogeneity (Cochran, 1954) and the I^2 statistic (Higgins & Thompson, 2002) are reported. In case any amount of heterogeneity is detected (i.e., $\tau^2 > 0$, regardless of the results of the Q -test), a prediction interval for the true outcomes is also provided (Riley et al., 2011). Studentized residuals and Cook's distances are used to examine whether studies may be outliers and/or influential in the context of the model (Viechtbauer & Cheung, 2010). Studies with a studentized residual larger than the $100 \times (1 - 0.05/(2 \times k))$ th percentile of a standard normal distribution are considered potential outliers (i.e., using a Bonferroni correction with two-sided $\alpha = 0.05$ for k studies included in the meta-analysis). Studies with a Cook's distance larger than six times the quantile range of the Cook's distances are considered to be influential. The rank correlation test (Begg & Mazumdar, 1994) and the regression test (Sterne & Egger, 2005), using the standard error of the observed outcomes as predictor, are used to check for funnel plot asymmetry. The analysis was carried out using R (version 4.0.3) (R Core Team, 2020) and the metafor package (version 2.5.70) (Viechtbauer, 2019).

Results

A total of $k = 13$ studies were included in the analysis. The observed log risk ratios ranged from -1.62 to 0.4459 , with the majority of estimates being negative (85%). The estimated average log risk ratio based on the random-effects model was $\bar{\mu} = -0.7145$ (95% CI: -1.0609 to -0.3622). Therefore, the average outcome differed significantly from zero ($z = -3.9744$, $p < 0.0001$). A forest plot showing the observed outcomes and the estimate based on the random-effects model is shown in Figure 1.

Demo: Using reporter()

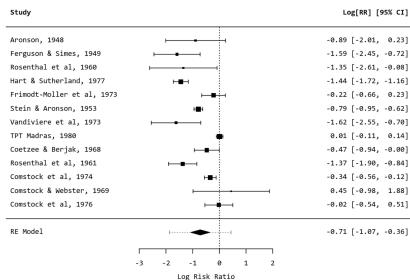


Figure 1: Forest plot showing the observed outcomes and the estimate of the random-effects model

According to the Q -test, the true outcomes appear to be heterogeneous ($Q(12) = 152.2330$, $p < 0.0001$, $I^2 = 0.3132$, $I^2 = 92.2214\%$). A 95% prediction interval for the true outcomes is given by -1.8667 to 0.4376 . Hence, although the average outcome is estimated to be negative, in some studies the true outcome may in fact be positive.

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Demo: Using reporter()

An examination of the studentized residuals revealed that none of the studies had a value larger than ± 2.8905 and hence there was no indication of outliers in the context of this model. According to the Cook's distances, none of the studies could be considered to be overly influential.

A funnel plot of the estimates is shown in Figure 2. Neither the rank correlation nor the regression test indicated any funnel plot asymmetry ($p = 0.9524$ and $p = 0.4218$, respectively).

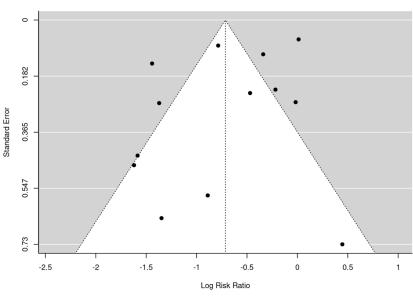


Figure 2: Funnel plot

Demo: Using reporter()

Notes

This analysis report was dynamically generated for model object 'res' with the `reporter()` function of the `metafor` package. The model call that was used to fit the model was: `rma(yi = yi, vi = vi, data = dat)`. This report provides an illustration of how the results of the model can be reported, but is not a substitute for a careful examination of the results.

References

- Begg, C. B., & Mazumdar, M. (1994). Operating characteristics of a rank correlation test for publication bias. *Biometrics*, 50(4), 1088–1101. <https://doi.org/10.2307/2533446>
- Cochran, W. G. (1954). A generalization of the combination of estimates from different experiments. *Biometrics*, 10(1), 101–129. <https://doi.org/10.2337/2001696>
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- Viechtbauer, W. (2005). Bias and efficiency of meta-analytic variance estimators in the random-effects model. *Journal of Educational and Behavioral Statistics*, 30(3), 261–293. <https://doi.org/10.3102/1076998603003261>
- Viechtbauer, W. (2010). Conducting meta-analyses in R with the `metafor` package. *Journal of Statistical Software*, 36(3), 1–48. <https://doi.org/10.18637/jss.v036.i03>
- Viechtbauer, W., & Cheung, M. W.-L. (2010). Outlier and influence diagnostics for meta-analysis. *Research Synthesis Methods*, 1(2), 112–125. <https://doi.org/10.1002/rsmi.111>

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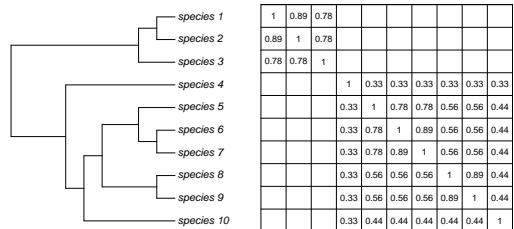
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Validation / Testing

- extensive comparisons with other R/software packages
- comparisons with published results (e.g., [analysis examples](#))
- testing via simulation studies
- appreciable user base
- automated testing + code coverage (~70%)
- plus a 100% money-back guarantee if you find a bug!

Phylogenetic Meta-Analysis [22–24]

- meta-analyses in ecology and evolutionary biology often contain studies conducted with different species
- these species share an evolutionary history (= phylogeny)
- effects for species that are more similar to each other might also correlate more strongly

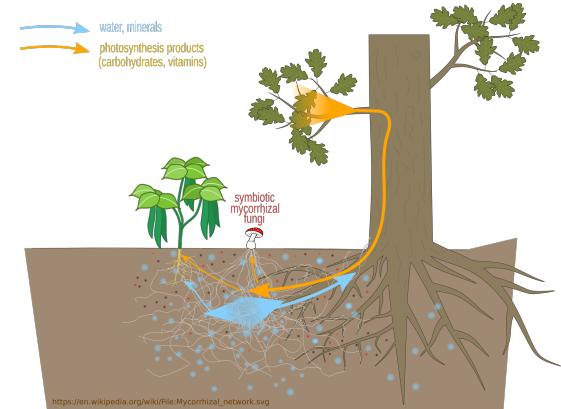


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Phylogenetic Meta-Analysis [22–24]

- in 2012, I was invited by Jason Hoeksema (University of Mississippi) to participate in a NESCent (National Evolutionary Synthesis Center) working group to develop methods/software for phylogenetic meta-analysis
- over the course of 5 meetings developed `rma.mv()` and its ability to incorporate known correlation matrices
- applied in a meta-analysis on the effects of inoculating plants with mycorrhizal fungi [25, 26]



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Effects of Mycorrhizal Fungi Inoculation

- focus here on plants inoculated with arbuscular mycorrhizal fungi belonging to one or more fungal genera (359 papers, 2984 effects, 1776 control conditions, 293 plant species)
- model includes random effects for papers, control conditions, effect sizes, plant species, and plant species with its phylogenetic correlation matrix

```
rma.mv(EffectSize, Var, data = dat,
       random = list(~ 1 | Paper/Control/Effect,
                     ~ 1 | PlantSpecies,
                     ~ 1 | PlantSpecies.phyl),
       R = list(PlantSpecies.phyl=R.PS))
```

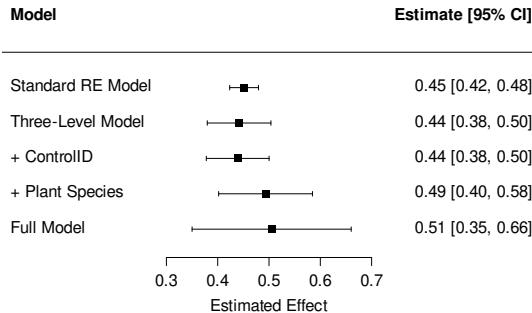
Effects of Mycorrhizal Fungi Inoculation

```
## Multivariate Meta-Analysis Model (k = 2984; method: REML)
##
## Variance Components:
##
##          estim      sqrt    nlvls   fixed     factor      R
## sigma^2.1  0.1799  0.4242    359    no   PaperID    no
## sigma^2.2  0.1434  0.3786   1776    no  ControlID   no
## sigma^2.3  0.1224  0.3498   2984    no   EffectID   no
## sigma^2.4  0.1618  0.4023    293    no PlantSpecies  no
## sigma^2.5  0.1000  0.3162    293    no PlantSpecies.phyl yes
##
## Test for Heterogeneity:
## Q(df = 2983) = 66515.4758, p-val < .0001
##
## Model Results:
##
##          estimate      se     zval   pval  ci.lb  ci.ub
## 0.5051  0.0791  6.3858 <.0001  0.3501  0.6601
```

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Effects of Mycorrhizal Fungi Inoculation

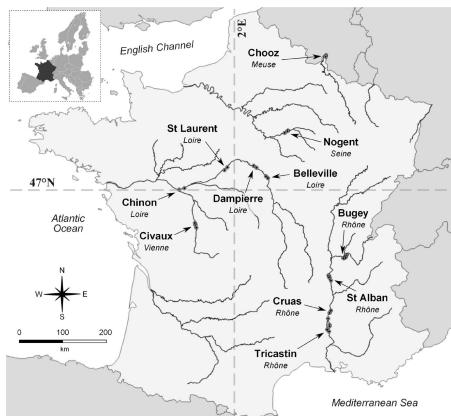


Spatial Correlation Structures in Meta-Analysis

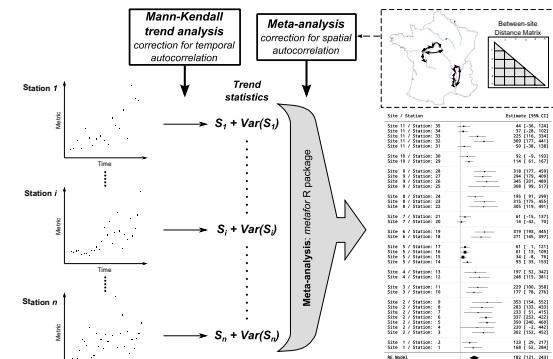
- was contacted in 2017 by researchers doing a meta-analysis on changes in fish abundance/diversity in French rivers
- had derived trend statistics based on repeated measures of fish abundance/diversity at 35 sampling stations (11 general sites)
- expected strong spatial correlation in these trend estimates
- implemented spatial correlation structures in `rma.mv()` to account for this and helped with the analysis [27]

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Trends in Fish Abundance/Diversity in French Rivers

- 35 × 35 distance matrix derived based on the 'river distance' between the stations (min = 1km, max = 423km)
- pairs of stations not connected through the river network assumed to be uncorrelated



Trends in Fish Abundance/Diversity in French Rivers

- Gaussian spatial correlation structure: $\text{Cov}[u_i, u_j] = \tau^2 \times \exp(-d_{i,j}^2/\rho^2)$, where $d_{i,j}$ is their distance
- model includes random effects for sites, stations, and correlated random effects for stations assuming an exponential or Gaussian spatial correlation structure

```
rma.mv(EffectSize, Var, data = dat,
        random = list(~ 1 | site/station,
                      ~ station | const),
        struct="SPGAU", dist=list(dmat))
```

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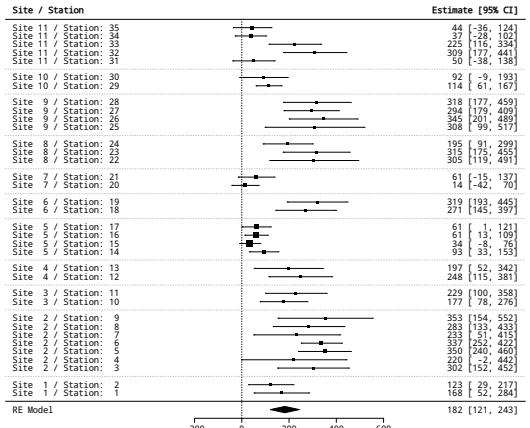
Trends in Fish Abundance/Diversity in French Rivers

```

## Multivariate Meta-Analysis Model (k = 35; method: REML)
##
## Variance Components:
##
##          estim   sqrt  nlvls fixed     factor
## sigma^2.1 7158.35 84.61    11    no      site
## sigma^2.2   0.00  0.00    35    no site/station
##
## outer factor: const (nlvls = 1)
## inner term: -station (nlvls = 35)
##
##          estim   sqrt  fixed
## tau^2     3425.59 58.53    no
## rho       12.88    no
##
## Model Results:
##
## estimate   se   zval pval ci.lb ci.ub
## 182.12 31.28 5.82 <.01 120.81 243.43

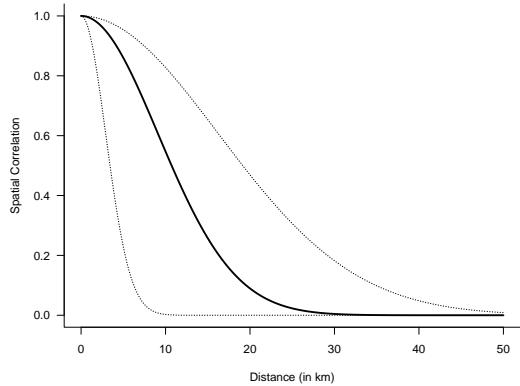
```

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Trends in Fish Abundance/Diversity in French Rivers



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Complex Random-Effects Structures

- 2016-2020 I was involved in a meta-analysis on the 'generation effect' (= information is better remembered if it is generated from one's own mind rather than simply read) [28]
- a study might ask participants to recall words that were read versus words self-generated from word fragments
- studies often report multiple experiments and examine various conditions using a mix of within- and between-subject designs

Complex Random-Effects Structures

Article	Experiment	Sample	Pairing	Condition	Id	Recall
1	1	1	1	read	1	0.31
1	1	2	1	generate	2	0.45
2	1	3	2	read	3	0.45
2	1	3	2	generate	4	0.61
3	1	4	3	read	5	0.61
3	1	4	3	generate	6	0.72
3	1	4	3	generate	7	0.95
4	1	5	4	read	8	0.28
4	1	5	4	generate	9	0.38
4	1	6	5	read	10	0.36
4	1	6	5	generate	11	0.55
...

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Complex Random-Effects Structures

- dataset included 126 articles reporting on 310 experiments with 582 samples, yielding 1653 recall estimates for 804 pairings
- model includes random effects for articles, experiments, samples, estimates, and a crossed random effect for pairing
- so a five-level model with an additional crossed random effect

```
rma.mv(Recall, Var, mods = ~ Condition,
        random = list(~ 1 | article/experiment/sample/id,
                      ~ 1 | pairing),
        data=dat, sparse=TRUE)
```

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Complex Random-Effects Structures

```

## Multivariate Meta-Analysis Model (k = 1653; method: REML)
##
## Variance Components:
##
##          estim   sqrt  nlvls fixed     factor
## sigma^2.1 0.0219 0.1479    126   no Article
## sigma^2.2 0.0060 0.0777    310   no Experiment
## sigma^2.3 0.0000 0.0000    582   no Sample
## sigma^2.4 0.0064 0.0798   1653   no Id
## sigma^2.5 0.0165 0.1285    804   no Pairing
##
## [...]
##
## Model Results:
##
##          estimate      se     zval   pval ci.lb ci.ub
## intrcpt  0.4785 0.0157 30.4456 <.0001 0.4477 0.5093
## generate  0.1021 0.0042 24.0422 <.0001 0.0938 0.1104

```

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Sparse Matrix Structures

- `rma.mv()` works by default internally with $k \times k$ matrices, where k denotes the number of rows in the dataset
- model fitting can be painfully slow when k is large
- was contacted around 2013 about this issue by people from Vanderbilt University (i.e., Joshua Polanin, Mark Lipsey and Sandra Wilson) who were running models with $k > 8000$ rows!
- this led to the implementation of the `sparse=TRUE` option so ‘sparse matrix representations’ are used to speed things up

$$W = \begin{bmatrix} a & b & | & 0 & 0 \\ c & d & | & 0 & 0 \\ \hline 0 & 0 & | & e & f \\ 0 & 0 & | & g & h \end{bmatrix}^{-1} = \begin{bmatrix} [a & b]^{-1} & & & & \\ [c & d]^{-1} & & & & \\ \cdot & & \cdot & & \\ \cdot & & \cdot & & [e & f]^{-1} \\ \cdot & & \cdot & & [g & h]^{-1} \end{bmatrix}$$

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Philosophy

- build a toolbox, not individuals tools
- try to avoid special cases / figure out logical generalizations
- coherent and general modeling framework; e.g., `rma.mv()` for:
 - multilevel meta-analysis (e.g., [29], [website](#))
 - multivariate meta-analysis (e.g., [30], [website](#))
 - network meta-analysis (e.g., [ex 1](#), [ex 2](#), [ex 3](#), [ex 4](#))
 - phylogenetic meta-analysis (e.g., [24])
 - spatio-temporal models (e.g., [27])
 - dose-response models
 - all can be combined with (cluster) robust variance estimation (using `robust()` or the `clubSandwich` package)
- listen to users

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Thank You for Your Attention!

Questions, Comments, Suggestions?

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